INSTITUTE OF MATHEMATICS

College of Science University of the Philippines Diliman

Math 23 Course Syllabus

A. Course Catalogue Description

Course Number Math 23

Course Title Elementary Analysis III

Course Description Functions of several variables; limits and continuity of functions of several

variables; partial derivatives and the total differential; directional derivatives; relative and absolute extrema of functions of several variables; double and triple integrals; applications of multiple integrals; vector fields; line and

surface integrals

Prerequisite Math 22/equiv.

Course Credit 4 units

Number of Hours 4 hours/week

B. Course Content

- I. Course Introduction
- II. Differential calculus of functions of several variables
 - 1. Functions of several variables, level curves, and level surfaces
 - 2. Limits and continuity of functions of several variables
 - 3. Partial derivatives
 - 4. Higher-order derivatives, the total differential, and tangent plane approximation
 - 5. The Chain Rule and implicit differentiation
 - 6. Directional derivatives and gradients
 - 7. Tangent planes to level surfaces
 - 8. Relative extrema and the Second Derivative Test
 - 9. Absolute extrema and the method of Lagrange multipliers
 - 10. Parametric surfaces and surfaces of revolution

III. Multiple Integration

- 1. Double integrals
- 2. Double integrals in polar coordinates
- 3. Applications of double integrals (area, volume, mass, surface area)
- 4. Triple integrals
- 5. Triple integrals in cylindrical and spherical coordinates
- 6. Applications of triple integrals (volume, mass)
- IV. Vector fields, line integrals and surface integrals
 - 1. Vector fields
 - 2. Curl and divergence
 - 3. Line integrals of scalar and vector fields
 - 4. The Fundamental Theorem of Line Integral
 - 5. Path-independent line integrals
 - 6. Green's Theorem
 - 7. Surface integrals of scalar and vector fields
 - 8. Stokes' Theorem and Gauss' Divergence Theorem

For a more detailed syllabus, send an email request to ddapr@math.upd.edu.ph.