INSTITUTE OF MATHEMATICS College of Science University of the Philippines Diliman

Math 128 Course Syllabus

A. Course Catalogue Description

Math 128
Complex Analysis
Complex numbers and properties; analytic functions and the Cauchy-
Riemann equations; power series representation of analytic functions; com-
plex integration; Cauchy integral formula and its consequences; singulari-
ties, Laurent series, and residues; applications to definite integrals
Math 123.1/equiv.
3 units
3 hours/week

B. Course Content

- I. Course Introduction and Orientation
- II. Complex Numbers
 - 1. Representations and properties of a complex number
 - 2. Powers and roots of complex numbers
 - 3. The point of infinity and topological notions in the extended complex plane
- III. Complex Functions
 - 1. Images of curves under elementary mappings
 - 2. Exponential and related functions
 - 3. Multiple-valued functions and branch cuts
 - 4. Limits and continuity
 - 5. Derivative of a complex function
 - 6. Analyticity and Cauchy-Riemann equations
- IV. Complex Series
 - 1. Sequences and series
 - 2. Power series and its radius of convergence
 - 3. Analyticity of power series
- V. Complex Integration
 - 1. Contour integrals and its properties
 - 2. ML-Inequality Estimate
 - 3. Cauchy-Goursat Theorem and Independence of Path
- VI. Cauchy Integral Formula and its Consequences
 - 1. Cauchy's integral formula
 - 2. Estimates of derivative of analytic functions
 - 3. Power series representation of analytic functions
 - 4. Liouville's theorem and the fundamental theorem of algebra
 - 5. Uniqueness and identity theorems
 - 6. Maximum modulus principle
- VII. Singularities and Residues
 - 1. Classification of isolated residues
 - 2. Laurent series representation of meromorphic functions
 - 3. Cauchy's residue theorem
 - 4. Argument Principle and Rouché's theorem
 - 5. Evaluation of improper integrals

For a more detailed syllabus, send an email request to ddapr@math.upd.edu.ph.