### INSTITUTE OF MATHEMATICS College of Science University of the Philippines Diliman

#### Math 122 Course Syllabus

## A. Course Catalogue Description

Course Number	Math 122
Course Title	Differential Equations and Applications
Course Description	First order ordinary differential equations (ODEs); homogeneous and non-
	homogeneous linear second order ODEs; systems of linear equations; series
	solutions of ODEs; stability analysis of nonlinear ODEs; Laplace trans-
	forms; applications of ODEs
Prerequisite	Math 22/equiv. or Math 30/equiv.
Course Credit	3 units
Number of Hours	3 hours/week

# **B.** Course Content

- I. Course Introduction and Orientation
- II. First Order Differential Equations
  - 1. Definition and Examples of Differential Equations
  - 2. Families of Curves
  - 3. Existence and Uniqueness of Solutions
  - 4. Separable Equations
  - 5. Exact Equations
  - 6. Integrating Factors
  - 7. Substitution Methods
    - a. Equations with homogeneous coefficients
    - b. Equations with linear coefficients
    - c. Bernoulli's equation
  - 8. Applications
    - a. Population Models
    - b. Acceleration-Velocity Models
- III. Linear (Homogeneous) Differential Equations of Higher Order
  - 1. Existence and Uniqueness of Solutions
  - 2. Linear independence of solution and the Wronskian
  - 3. General Solutions of Linear DE's
  - 4. Differential Operators
  - 5. Homogeneous Equations with Constant Coefficients
- IV. Linear (Nonhomogeneous) Differential Equations of Higher Order
  - 1. Method of Undetermined Coefficients
  - 2. Variation of Parameters
  - 3. Applications
    - a. Undamped Vibrations
    - b. Damped Vibrations and Resonance
    - c. Electrical Circuits
  - 4. Endpoint Problems and Eigenvalues
- V. Power Series Methods
  - 1. Power series representation of elementary functions
  - 2. Series solutions near ordinary points

## VI. Laplace Transform Methods

- 1. Definition of Laplace Transform and Inverse Laplace Transform
- 2. Transforms of Derivatives
- 3. Derivatives of Transforms
- 4. Translation and Partial Fractions
- 5. Solving Differential Equations using Laplace Transform
- VII. Linear Systems of Differential Equations
  - 1. First-order differential systems with constant coefficients
  - 2. Method of Elimination
  - 3. Matrices and Linear Systems
  - 4. Eigenvalue Method for Homogeneous Systems
  - 5. Nonhomogeneous Linear Systems
- VIII. Introduction to Nonlinear Systems

For a more detailed syllabus, send an email request to ddapr@math.upd.edu.ph.