INSTITUTE OF MATHEMATICS

College of Science University of the Philippines Diliman

Math 110.3 Course Syllabus

A. Course Catalogue Description

Course Number Math 110.3

Course Title Abstract Algebra III

Course Description Polynomial rings and factorization; field extensions, splitting fields, finite

fields, field automorphisms; introduction to Galois theory

Prerequisite Math 110.1 Course Credit 3 units Number of Hours 3 hours/week

B. Course Content

I. Course Introduction and Orientation

- II. Introduction to Rings and Fields
 - 1. Rings of Polynomials
 - 2. Factorization of Polynomials over a Field
- III. Factor Rings and Ideals
 - 1. Homomorphism and Factor Rings
 - 2. Prime and Maximal Ideals
- IV. Factorization
 - 1. Unique Factorization Domains
 - 2. Euclidean Domains and Principal ideal domains
 - 3. Gaussian Integers and Norms
- V. Extension Fields
 - 1. Introduction to Extension Fields
 - 2. Review on Vector Spaces
 - 3. Algebraic Extensions
 - 4. Geometric Constructions
 - 5. Finite Fields
- VI. Automorphisms and Galois Theory
 - 1. Automorphisms of Fields
 - 2. The Isomorphism Extension Problem
 - $3. \ \, {\rm Splitting} \,\, {\rm Fields}$
 - 4. Separable Extensions
 - 5. Galois Theory
 - 6. Illustrations of Galois Theory
 - 7. Cyclotomic Extensions

For a more detailed syllabus, send an email request to ddapr@math.upd.edu.ph.