#### INSTITUTE OF MATHEMATICS

College of Science University of the Philippines Diliman

# Math 110.1 Course Syllabus

## A. Course Catalogue Description

Course Number Math 110.1

Course Title Abstract Algebra I

Course Description Groups, group homomorphism; permutation groups; factor groups; rings,

ring homomorphism, ideals, integral domains; introduction to fields, field

of quotients

Prerequisite Math 108/equiv. or COI

Course Credit 3 units

Number of Hours 3 hours/week

#### **B.** Course Content

I. Course Introduction and Orientation

#### II. Preliminaries

- 1. Equivalence Relations
- 2. Binary Operations
- 3. Division Algorithm
- 4. Modular Arithmetic

### III. Groups

- 1. Definition and elementary properties of groups
- 2. Group tables
- 3. Order of a group and subgroups
- 4. Lattice diagram of a group
- 5. Isomorphism of groups
- 6. Cyclic groups and subgroups
- 7. The groups Z and  $Z_k$
- 8. Cosets and the Theorem of Lagrange

# IV. More Groups and Direct Products

- 1. Permutation groups
- 2. Orbits, cycles and transpositions
- 3. Direct products
- 4. Subgroups generated by a subset
- 5. Finitely generated abelian group

# V. Homomorphisms and Factor Groups

- 1. Definition and properties
- 2. Kernel and image
- 3. Normal subgroups
- 4. Factor groups

# VI. Rings

- 1. Definition and properties of rings
- 2. Commutative rings
- 3. Rings with unity
- 4. Groups and units of a ring
- $5.\,$  Subrings, ideals and factor rings

# VII. Ring Homomorphisms and Fields

- $1. \ \, {\rm Ring} \,\, {\rm Homomorphism} \,\, {\rm Theorems}$
- 2. Zero divisors
- 3. Characteristic of a ring
- 4. Integral domains
- 5. Fields
- 6. Field of Quotients

For a more detailed syllabus, send an email request to ddapr@math.upd.edu.ph.